

MATH 115  
Exam II

Name \_\_\_\_\_

1. Differentiate

a)  $f(x) = 3x^5 + 5\sqrt{x} + \frac{8}{x}$

b)  $g(t) = e^{3t+1} + 2^t$

2. Differentiate

a)  $f(x) = \ln(1 + e^{-x})$

b)  $g(x) = \sin(x^2 + \ln x)$

3. Find the equation of the line tangent to  $y = 2x^3 - 5x^2 + 3x - 5$  at  $x = 1$ .

4. Assume the demand function for a certain product is given by  $q = 1000e^{-.02p}$  where  $p$  is the price of the product in dollars and  $q$  is the quantity sold at that price.

a) Write revenue  $R$  as a function of price.

b) Find the rate of change of revenue with respect to price.

5. Choose the constants  $a$  and  $b$  in the function  $f(x) = axe^{bx}$  such that  $f(\frac{1}{3}) = 1$  and the function has a maximum at  $x = \frac{1}{3}$ .

6. Sketch a possible graph of a function  $f(x)$  with the following properties:

a)  $f'(x) > 0$  for  $x < 2$

b)  $f'(2) = 0$

c)  $f'(x) > 0$  for  $2 < x < 5$

d)  $f'(5) = 0$

e)  $f'(x) < 0$  for  $x > 5$

7. Assume the cost function for a product is given by  $C(q) = .04q^3 - 3q^2 + 75q + 96$  dollars where  $q$  is the number of items produced. Find the minimum average cost.

8. Find the points on the graph of  $y = \frac{x^2+3x-1}{x}$  where the slope is 5.

9. A small shop sells ties for \$3.50 each. The daily cost function is estimated to be  $C(x)$  dollars where  $x$  is the number of ties sold on a typical day and  $C(x) = .0006x^3 - .03x^2 + 2x + 20$ . Find the value of  $x$  that will maximize the store's daily profit.

10. A boat at anchor is bobbing up and down in the sea. The vertical distance  $y$ , in feet, between the sea floor and the boat is given as a function of time  $t$ , in minutes, by  $y = 15 + \sin(2\pi t)$ . Find the vertical velocity of the boat at time  $t$ .