

# Math 223 Exam#3

Name \_\_\_\_\_

I.D. # \_\_\_\_\_

1. (12 pts) Let  $D$  be the region inside the circle  $x^2 + y^2 = 1$ . Decide whether each integral is positive, negative, or zero.

(a)  $\int_D \sin x dA$

(b)  $\int_D \sin(x^2) dA$

(c)  $\int_D xy dA$

(d)  $\int_D e^{-y^2} dA$

2. (10 pts) Evaluate the integral  $\int_R (2x^2y + 3) dA$ , where  $R$  is the region bounded by  $y = x$  and  $y = x^2$ .

3. (8 pts) Reverse the order of the integration of the integral  $\int_0^1 \int_{\sqrt{y}}^1 e^{x^3} dx dy$

4. (6 pts) Evaluate the integral  $\int_0^1 \int_{\sqrt{y}}^1 e^{x^3} dx dy$

5. (6 pts) Sketch the region over which the integral  $\int_0^1 \int_{x^2}^{\sqrt{x}} f(x, y) dx dy$  is computed.
6. (4 pts) Sketch the region over which the integral  $\int_0^{\pi/4} \int_0^5 f(r, \theta) r dr d\theta$  is computed.
7. (8 pts) Evaluate  $\int_R (x^2 + y^2)^{1/2} dA$ , where  $R$  is the upper half of the ring bounded by  $x^2 + y^2 = 9$  and  $x^2 + y^2 = 4$ .
8. (8 pts) Convert the integral  $\int_{-2}^2 \int_0^{\sqrt{4-x^2}} \cos(x^2 + y^2) dy dx$  to polar coordinates and evaluate.
9. (6 pts) Write a parameterization of the circle of radius 5 centered at the origin traced clockwise starting from  $(0, 5)$  when  $t = 0$ .

10. (6 pts) Write a parameterization of the line through the points  $(1, -1, 2)$  and  $(-1, 0, 3)$ .

11. (6 pts) Find the acceleration vectors for the motion 
$$\begin{cases} x = t^3 + 2t - 3 \\ y = t^2 - 2t + 3 \\ z = t + 4 \end{cases}$$

12. (8 pts) Find the length of the curve 
$$\begin{cases} x = 1 - t \\ y = 2 + t \\ z = 3 - t \end{cases} \text{ for } 0 \leq t \leq 4.$$

13. (6 pts) Find a normal vector of the plane 
$$\begin{cases} x = 4 + s - 2t \\ y = 5 - s \\ z = 6 + t \end{cases}$$

14. (6 pts) Are the line 
$$\begin{cases} x = 5 - 2t \\ y = 7 + 2t \\ z = 9 + 4t \end{cases}$$
 and the plane  $x - y - 2z = 99$  perpendicular, parallel, or neither?